

Faraday's law

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Maxwell's equations describing Electrodynamics

- Gauss's law

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \quad (1)$$

- Faraday's law

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \quad (2)$$

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$$\nabla \cdot \mathbf{B} = 0 \quad (3)$$

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$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \quad (4)$$

where sources ρ and \mathbf{J} are charge density and current density respectively.

Faraday's Law: Experimental observations

A current flows in a loop:

- When the loop of wire is pulled to the right through a magnet.
- When the magnet itself moved to left, holding the loop.
- With both the loop and the magnet at rest, but varying the strength of field.

A changing magnetic field induces an electric field.

- Mathematically, the above observations can be expressed as

$$\mathcal{E} = -\frac{d\phi}{dt}, \quad (5)$$

that says the induced emf \mathcal{E} is equal to the rate change of the flux ϕ .

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- Whenever (and for whatever reason) the magnetic flux through a loop changes an emf

$$\mathcal{E} = -\frac{d\phi}{dt}, \quad (6)$$

will appear in the loop.

Integral & Differential form of the Faraday's law

- The induced electric field is given by the line integral

$$\mathcal{E} = - \oint E \cdot dl, \quad (7)$$

and then E is related to the change in B as

$$\oint E \cdot dl = - \oint \frac{\partial B}{\partial t} \cdot da, \quad (8)$$

- The Eq. (8) is the integral form of the Faraday's law.
- Using Stokes's theorem, this further reduces to differential form

$$\nabla \times E = - \frac{\partial B}{\partial t}. \quad (9)$$

Reference

- D. J. Griffiths, *Introduction to Electrodynamics*, Prentice Hall (1999).